

## FUNCTIONAL SKILLS CERTIFICATE Functional Mathematics

Level 1

Mark Scheme

4367

November 2017

Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aga.org.uk

## **Glossary for Mark Schemes**

Examinations are marked to award positive achievement.

Marks are awarded for demonstrating the following interrelated process skills.

**Representing** Selecting the mathematics and information to model a situation.

- **R.1** Candidates recognise that a situation has aspects that can be represented using mathematics.
- **R.2** Candidates make an initial model of a situation using suitable forms of representation.
- **R.3** Candidates decide on the methods, operations and tools, including ICT, to use in a situation.
- **R.4** Candidates select the mathematical information to use.

## **Analysing** Processing and using mathematics.

- **A.1** Candidates use appropriate mathematical procedures.
- **A.2** Candidates examine patterns and relationships.
- **A.3** Candidates change values and assumptions or adjust relationships to see the effects on answers in models.
- **A.4** Candidates find results and solutions.

## **Interpreting** Interpreting and communicating the results of the analysis.

- **I.1** Candidates interpret results and solutions.
- **I.2** Candidates draw conclusions in light of situations.
- **1.3** Candidates consider the appropriateness and accuracy of results and conclusions.
- **I.4** Candidates choose appropriate language and forms of presentation to communicate results and solutions.

In particular, individual marks are mapped onto the following skills standards.

**Representing** Making sense of the situations and representing them.

A learner can:

Ra Understand routine and non-routine problems in familiar and

unfamiliar contexts and situations.

**Rb** Identify the situation or problems and identify the mathematical

methods needed to solve them.

**Rc** Choose from a range of mathematics to find solutions.

**Analysing** Processing and using the mathematics.

A learner can:

**Aa** Apply a range of mathematics to find solutions.

**Ab** Use appropriate checking procedures and evaluate their

effectiveness at each stage.

**Interpreting** Interpreting and communicating the results of the analysis.

A learner can:

Interpret and communicate solutions to multistage practical problems in familiar and unfamiliar contexts and situations.

**Ib** Draw conclusions and provide mathematical justifications.

To facilitate marking, the following categories are used:

M Method marks are awarded for a correct method which could lead to a

correct answer.

A Accuracy marks are awarded when following on from a correct

method. It is not necessary to always see the method. This can be

implied.

**B** Marks awarded independent of method.

Ft Follow through marks. Marks awarded following a mistake in an

earlier step.

SC Special case. Marks awarded within the scheme for a common

misinterpretation which has some mathematical worth.

Oe Or equivalent. Accept answers that are equivalent.

Eg, accept 0.5 as well as  $\frac{1}{2}$ 

Q	Answer	Mark	Comments
1(0)	1.5 × 30	M1 Rc	
1(a)	45	A1 Aa	
1(a) check	Reverse or alt calculation eg $45 \div 30 = 1.5$ or $45 \div 1.5 = 30$ or $30 + 15 = 45$	B1ft <i>Ab</i>	
	Ac	ditional	Guidance
1(a)	If starting from 288 litres for 32 flushes the complete method must be seen for M1 $ (288 \div 32) \times 30 = 270 $ and $ ((288 \div 32) - 1.5) \times 30 = 225 $ and their 270 – their 225  oe eg seeing 9 for 288 $\div$ 32 Further work seen is A0 eg 1.5 $\times$ 30 = 45, 288 – 45 = 243 M1A0		

Q	Answer	Mark	Comments
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	Alternative method 1				
	3 x 77 or 231	M1 Rb			
	216 ÷ 6 × 3 or 216 ÷ 2 or 108	M1 Rb			
	their 231 – their 108 or their 108 + 120 or 228	M1 Aa	baths – showers		
1(b)	123 and Yes or 231 and 228 and Yes	A2 /	A1 123 or A1 231 and 228 A1ft Correct conclusion for their value(s) if 3rd M1 awarded		
	Alternative method 2				
	216 ÷ 6 or 36	M1 Rb			
	77 – their 36 or 41	M1 Rb	bath – shower		
	3 × their 41 or 120 ÷ their 41	M1 Aa	their 41 must be bath – shower		
	123 and Yes or 2.9 and Yes	A2 /	A1 123 or 2.9 A1ft Correct conclusion for their value if 3rd M1 awarded		
		Additional	Guidance		

Q Answer	Mark	Comments
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	Alternative meth	od 1			
	600 x 365 = 219 000 and 219 000 ÷ 1000 = 219  Alternative methor	600 ÷ 1000 = 0.6 and 0.6 × 365 = 219	B2 Rc Aa	B1 600 x 365 = 219 000 or 600 ÷ 1000 = 0.6	
1(c)	219 x 1000 = 219 000 and 219 000 ÷ 365 = 600	219 × 1000 = 219 000 and 219 000 ÷ 600 = 365	B2 Rc Aa	B1 219 × 1000 = 219 000	
	Additional Guidance				
	Division or multiplication by 1000 must be shown eg $600 \times 365 = 219\ 000 = 219\ \text{litres}$ Allow starting at both ends eg $600 \times 365 = 219000$				B1
	and 219 x 1000 =				B2

Q	Answer	Mark	Comments		
	Alternative method 1				
	219 × 3 or 657	M1 Ra			
	their 657 + 125 or their 657 + 125 – 720 or 720 – their 657	M1 Rb	their 657 cannot be 3 or from 1 720 × 3 or 1000 × 3	25 × 3 or	
1(d)	782 and No or 62 and No or 63 and No	A2 /	A1 782 or 62 or 63 A1ft Correct conclusion for thei 2nd M1 awarded	r value if	
	Alternative method 2				
	219 × 3 or 657	M1 Ra			
	720 – 125 or 595	M1 Rb			
	595 and 657 and No  A2  /  A1 595 and 657  A2  /  A1ft Correct conclusion for			r values	
	Ac	ditional (	Guidance		
	Use of 219 000 instead of 219 can gain	n max 2 m	arks		
	219 000 × 3 = 657 000 657 000 + 125 = 657 125 and No	d as order		M0M1A0 A1ft	
	They must make a decision for the final mark eg It's £62 more expensive/cheaper eg No It's £62 more expensive eg 782 No, without a water meter would be cheaper			M2A1A0 M2A2 M2A2	

Q		Answer	Mark	Commer	nts
			Mark	Johnne	
	53.23		B1		
	55.25		Rb		
2(a)			Additional G	- Luidanco	
		· · · · · · · · · · · · · · · · · · ·			
	All correct				
	Lane 1	Dai		B2 one pair of swimmers rest correct	swapped with the
	Lane 2	Cheng		eg all correct except Kev i Ahmed in Lane 5	n Lane 3 and
	Lane 3	Ahmed		B1 Ahmed in Lane 3 and	Kev in Lane 5
	Lane 4	Jack (given)	B3 Ra,Rb,I	or	
	Lane 5	Kev		B1 all 8 correct names us	ed
	Lane 6	Paul			
	Lane 7	Zain			
2(b)	Lane 8	Tom			
	Additional Guidance				
	For the B2 for one pair swapped they can only be swapped with the next lane that would be allocated				
	The possible swaps are				
	Kev and Ahmed				
	Ahmed and Paul				
	Paul and Cheng				
	Cheng and Z	ain			
	Zain and Dai				
	Dai and Tom				

Q	Answer	Mark	Comments

	Alternative method 1				
	50.6 + 51.7 + 52.6 + 49.6 + 50.2 + 49.8 or 304.5	M1			
	or	Aa			
	50.2 + 49.6 + 51.2 + 48.2 + 49.5 + 51.3 or 300				
	50.6 + 51.7 + 52.6 + 49.6 + 50.2 + 49.8 or 304.5	M1			
	and	Aa			
	50.2 + 49.6 + 51.2 + 48.2 + 49.5 + 51.3 or 300	Ad			
	304.5 and 300 and Duncan	A2	A1 304.5 and 300		
2(c)		1,1	A1ft correct conclusion for their values		
	Alternative method 2				
	50.6 + 51.7 + 52.6 + 49.6 + 50.2 + 49.8 or 304.5	M1			
	or	Aa			
	50.2 + 49.6 + 51.2 + 48.2 + 49.5 + 51.3 or 300				
	their 304.5 ÷ 6 or 50.75	M1			
	or	Aa			
	their 300 ÷ 6 or 50				
	50.75 and 50 and Duncan	A2	A1 50.75 and 50		
		1,1	A1ft correct conclusion for their values		

Q	Answer	Mark	Comments
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	Alternative method 3		
	<b>Ben</b> 49.6, 49.8, 50.2, 50.6, 51.7, 52.6,		Arranges at least 4 in order from either end and indicates middle
	or	M1	
	Duncan	Aa	
	48.2, 49.5, 49.6, 50.2, 51.2, 51.3,		
	50.4	M1	
	or	Aa	
	49.9		
	50.4 and 49.9 and Duncan	A2	A1 50.4 and 49.9
		1,1	A1ft correct conclusion for their values
	Alternative method 4		
2(c) cont'd	compares number or proportion of times under 50 seconds	M1	
	eg Ben 2/6 or Duncan 3/6	Aa	
	Ben 2/6 and Duncan 3/6	M1 Aa	
	Duncan as he has more times under		A1 Duncan without clear explanation
	50 seconds/is more likely to swim under 50 seconds		A1ft correct conclusion for their values
			SC2 Choose Duncan as he won 5 of the races
		A2	or SC2 choose Duncan as Ben only won one of the races
		I,I	SC1 Duncan won 5 of the races/Ben only won one of the races
			SC2 compares quickest and/or slowest time and chooses Duncan
			SC1 compares quickest and/or slowest time

Q Answer	Mark	Comments
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	Additional Guidance	
	Note that the number of times under 51 seconds are the same for both swimmers	
	using alt 4 it must be clear that they are making a choice	
	examples	
	choose Duncan as he only had 3 swims over 50 secs but Ben had 4	M2A2
	Duncan had 3 swims over 50 secs and Ben had 4	M2 A0
2(c)		
	Examples of SC for comparing single values	
	Choose Duncan as he never swam slower than 52 seconds	SC2
	Duncan had the quickest time	SC1
	Choose Duncan as he had the quickest time	SC2
	Duncan is best as Ben had a time over 52 seconds but Duncan didn't	SC2

Q	Answer	Mark	Comments
	Alternative method 1		
	49.5(0) × 10 or 495	M1 Rc	
	7 × 5 or 35	M1 Aa	M2 for (7 + 58) × 5 or 325
	58 × 5 or 290	M1 Aa	
2(d)	their 495 + their 35 + their 290 or 820	M1 Aa	their values must be from an attempt at multiples of 49.5(0), 7 and 58 $49.5(0) + 7 + 58 (= 114.5) \text{ is M0}$
	their 820 ÷ 10 or 82	M1 Ra	M2 for their 820 × 0.9
	their 820 – their 82	M1 Aa	
	738 and Yes	Α2	A1 738

A2

1,1

A1ft correct conclusion for their value if 4th

method mark is awarded

Q	Answer	Mark	Comments
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	Alternative method 2		
	49.5(0) × 10 or 495	M1 Rc	
	7 × 5 or 35	M1 Aa	M2 for (7 + 58) × 5 or 325
	58 × 5 or 290	M1 Aa	
2(d) cont'd	their 495 ÷ 10 or 49.5 or their 35 ÷ 10 or 3.5 or their 290 ÷ 10 or 2.9	M1 Aa	
	their 495 – their 49.5 or 445.5(0) and their 35 – their 3.5 or 31.5(0) and their 290 – their 29 or 261	M1 Ra	At least two reductions by their 10% seen
	their 445.5(0) + their 31.5(0) + their 261	M1 Aa	Must be adding their 90% values or subtracts the sum of two of the values from 750 and compares with the third value
	738 and Yes	A2 <i>I,I</i>	A1 738 A1ft correct conclusion for their value if 6th method mark awarded

Q Answer	Mark	Comments
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	Alternative method 3		
	49.5(0) ÷ 10 or 4.95 or 7 ÷ 10 or 0.7 or 58 ÷ 10 or 5.8	M1 Ra	M2 for at least two of 49.5(0) × 0.9 or 44.55 and 7 × 0.9 or 6.3(0) and
2(d)	49.5 – their 4.95 or 44.55 and 7 – their 0.7 or 6.3(0) and 58 – their 5.8 or 52.2(0)	M1 Rc	58 × 0.9 or 52.2(0)  At least two reductions by their 10% seen
cont'd	their 44.55 × 10 or 445.5(0)	M1 Rc	
	their 6.3 × 5 or 31.5(0)	M1 Aa	M2 for (their 6.3 + their 52.2(0)) × 5 or 292.5(0)
	their 52.2(0) × 5 or 261	M1 Aa	
	their 445.5(0) + their 31.5(0) + their 261	M1 Aa	Must be adding their 90% values
	738 and Yes	A2 <i>I,I</i>	A1 738 A1ft correct conclusion for their value if 6th method mark awarded

Additional Guidance for this question is on the next page

Q Answer	Mark	Comments
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	Additional Guidance				
	For <b>Alt 2,</b> variations of the final M1 by subtracting 2 values from 750 and comparing what is left, can gain full marks				
	eg 750 – (their 445.5(0) + their 31.5(0)) = 273 and compares with 261				
	or				
	750 – (their 261 + their 31.5(0)) = 457.5 and compares with 445.5(0)				
	or				
	750 – (their 445.5(0) + their 261) = 43.5(0) and compares with 31.5(0) or with 35				
2(d)	(Note that as 43.5(0) is more than 35 they do not have to compare with the discounted amount)				
	Failing to work out 10% off £35 (as it does not affect the decision) needs justification for full marks				
	Example 1				
	445.5(0) + 261 + 35 =741.5(0) and Yes gains 7 marks (no justification for leaving 35 without the discount				
	Example 2				
	445.5(0) + 261 + 35 = 741.5(0) and states 'this is below £750 without deducting the 10% for the swim caps' gains 8 marks				

Q	Answer		Mark		Con	nments
	Eva on all six days on shift 1 only		B1 <i>Ra</i>			
	Cathy on all six days on shift 2 only		B1 <i>Rb</i>			
	Amy on every day	except Monday	B1 /			
	Ben on Mon, Thur	s and Friday only	B1 /			
	David on Mon, Tues, Wed and Sat only		B1 /			
	Additional Guidance					
3(a)	Example of a possible rota					
		Sh	Shift 1		Shift 2	
	Monday	Eva	Ben		Cathy	David
	Tuesday	Eva	David		Cathy	Amy
	Wednesday	Eva	David		Cathy	Amy
	Thursday	Eva	Ben		Cathy	Amy
	Friday	Eva	Ben		Cathy	Amy
	Saturday	Eva	David		Cathy	Amy
	Ignore repeats as	grid unless it is blank they will be penalise me in a cell not replac	-	-	_	ect were not crossed out

Q	Answer	Mark	Comments	
	24 × 7.5(0) or 180	M1		
2/h)		Rc		
3(b)	£180	A1	Must see £ symbol or 180 pounds	
		1		
3(b)	reverse or alt calculation	B1ft		
check	eg 180 ÷ 24 = 7.5	Ab		
	Additional Guidance			
	The £ sign (for 180) can be seen in the body of the script or the check –just needs to be seen once			
	eg			
	$24 \times 7.50 = 180$			
3(b)	check £180 $\div$ 7.50 = 24 M1/2	A1B1		
	If £180 seen and then further work, penalise the accuracy mark			
	eg $24 \times 7.5(0) = £180$ , £180 $\times 7 = £126$	60 M1A0	£ sign must be seen	
	eg $24 \times 7.5(0) = 180$ , $180 \times 7 = £1260$ could still be seen in the check and awa		(No £ sign seen here. However £180 nark)	

Q	Answer	Mark	Comments

	Alternative method 1				
	120 + 120 + 120 or 120 × 3 or 370 – 120 – 120 – 120	M1 Aa			
	360 and Yes	A2	A1 360		
	or He will have 10 spare/left	1,1	or A1ft correct conclusion for their value		
	Alternative method 2				
3(c)	370 ÷ 120	M1			
	or 370 ÷ 3	Aa			
	3.08 () and Yes		A1 3.08() or 3.1 or 123.3()		
	or 3.1 and Yes	A2	or A1ft correct conclusion for their value		
	or	1,1			
	123.3 () and Yes				
	Additional Guidance				
	Equivalent methods may be seen eg $370 - 120 - 120 = 130$ and Yes130 is bigger than 120. This would score full marks.				

Q	Answer	Mark	Comments

	Alternative method 1					
	5p – 1p or 4p or 460 × 5(p) or 2300	M1 Rb				
	460 × 4p or their 2300 – 460 or 1840	M1 Rc	460 × 4p is M1M1 Allow equivalent in pounds (18.40)			
	their 1840 ÷ 2 or 920 or their 1840 × 0.5(0)	M1 Aa				
	(£)9.20	A1 Aa				
	Alternative method 2					
3(d)	5p – 1p or 4p	M1 Rb				
	their 4p $\div$ 2 or their 4p $\times$ 0.5(0) or 2p	M1 Rc	4p ÷ 2 is M1M1  Allow equivalent in pounds (18.40)			
	their 2p × 460 or 920	M1 Aa				
	(£)9.20	A1 Aa				
	Alternative method 3					
	5p – 1p or 4p	M1 Rb				
	460 ÷ 2 or 460 × 0.5	M1 Rc				

Q	or 230 Answer	Mark	Comments

Q	Answer	Mark	Comments				
	their 230 × 4 or 920	M1					
		Aa					
	(£)9.20	A1					
		Aa					
	Ac	Additional Guidance					
3(d)	Allow work in pounds throughout eg 0.0						
cont'd	Forgetting to subtract the 1p per bag co						
	$eg 460 \times 5 = 2300$			M1			
	2300 ÷ 2= 1150			M0M1			
	£11.50			AO			
	Beware 460 ÷ 50 = 9.2 ans 9.20			МО			
	1121	B1					
4(a)		Rb					

**Additional Guidance** 

Q	Answer	Mark	Comments		
	2 × 40 + 2 × 60 or 80 + 120 or 200 or (40 + 60) × 2	M1 Ra			
	their 200 × 4 or 800	M1 Aa	or their 200 ÷ 150 or 1.3(3)		
	their 800 ÷ 150 or 5.3(3)  or  their 800 ÷ 5 or 160  or  5 × 150 or 750	M1 Rc	or their 1.3(3) × 4 their 800 cannot be 150		
4(b)	or 160 and No or 750 and 800 and No or (No) he is 50 (m) short  4(b)  A2 A1 750 and A1 ft correct and 3rd me For 5.3(3		A1 160 or A1 750 and 800	varded	
	Additional Guidance				
	Using area or half the perimeter can gain a maximum of M0M1M1A0A0  The 2nd and third method marks can be done in either order eg $200 \div 150 \times 4$ No can be implied eg he is 50 m short  Subtracting sides from 750 continuously can score full marks  eg $5 \times 150 = 750$ $750 - 40 - 40 - 60 - 60 - 40 - 40 - 60 - 6$			M1 M1M1 A2	

Q Answer	Mark	Comments
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	60 × 40 or 2400	M1 Ra			
	their 2400 ÷ 5 or 480 or their 2400 × 6 or 14400	M1 Aa			
	their 480 × 6 or their 14 400 ÷ 5 or 2880	M1 <i>Aa</i>			
4(c)	4840 ÷ 2 or 2420 or their 2880 × 2 or 5760 or their 2880 ÷ 4840	M1 <i>Rb</i>	their 2880 cannot be 240	0	
	2880 and 2420 and Yes or 460 yards extra or 5760 and Yes or 0.59(5) and Yes or 0.6 and Yes	A2 <i>I,I</i>	A1 2880 and 2420 or A1 5760 or A1 0.59(5) or 0.6 A1ft correct decision for th 3 method marks awarded	neir value(s) if first	
	Additional Guidance				
	Use of perimeter can gain max 3 mark eg 60 + 40 + 60 + 40 or 200 200 ÷ 5 or 40 40 × 6 or 240 4840 ÷ 2 or 2420 yes	S		M0 M1 M1 M1A0 A0ft as first M1 not awarded	

Q Answer	Mark	Comments
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	Sub-totals correct for all notes and coins	B2 Aa	B1 for at least two correct			
	Correct total for their six values + 20.00 + 13.18	B1ft Aa	ft their six sub-totals			
		Additional (	Guidance			
	£20	1		20.00		
	£10	2		20.(00)		
	£5	5		25.(00)		
	£2	1		2.(00)		
4(d)	£1	16		16.(00)	B3	
4(u)	50p	9		4.5(0)		
	20p	31		6.2(0)		
	Other coins			13.18		
	Assume integers are pounds eg 450  Just repeating the £10, £5 etc from the for the correct total of 51.88	·				